

Physics 661

Particle Physics Phenomenology

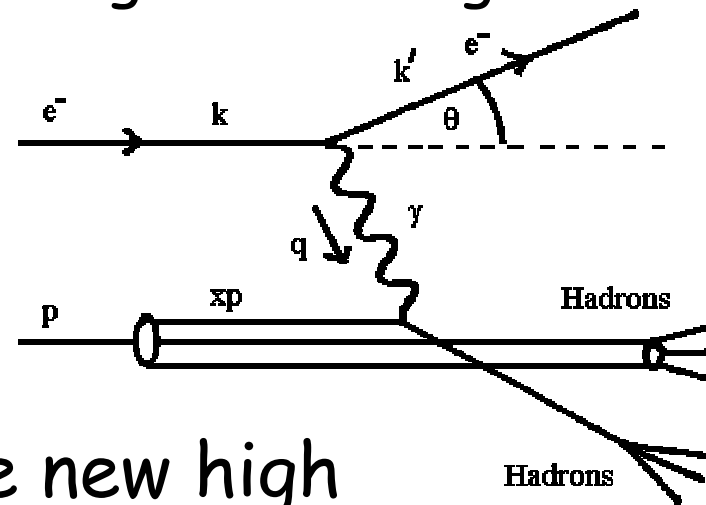
October 14, 2003

Quarks and Leptons

- Elem. Particles and High Energy Physics
- Fixed Targets and Colliding Beams
- The Standard Model
 - fundamental fermions, interactions, time scales
- Limitations of the Standard Model
- Fermions and Bosons
- Particles and Antiparticles
- Free Particles and their wave equations
- Helicity States
- Lepton Flavors
- Quark Flavors

Elementary particles and High Energy Physics

- In order to explore the substructure of matter we need to go to high energy
 - resolution is limited by deBroglie wavelength
 - $\lambda = h/p$



- Also, in order to produce new high mass particles we need higher energy

Fixed Target and Colliding Beam Accelerators

- Early experiments were done with a beam of particles and a fixed target

- The energy in the center-of-mass is

$$\begin{aligned}s \equiv E_{\text{cm}}^2 &= (E_{\text{beam}} + m_{\text{target}})^2 - p_{\text{beam}}^2 \\ &= 2 E_{\text{beam}} m_{\text{target}} + m_{\text{target}}^2 + m_{\text{beam}}^2\end{aligned}$$

- E_{cm} only increases as the square root of E_{beam}
(note $\sqrt{s} \equiv E_{\text{cm}}$)

- By colliding beams of particles,
 E_{cm} increases linearly with E_{beam}

$$\begin{aligned}s \equiv E_{\text{cm}}^2 &= (E_{\text{beam}} + E_{\text{beam}})^2 - (p_{\text{beam}} - p_{\text{beam}})^2 \\ &= 4 E_{\text{beam}}^2\end{aligned}$$

Colliding Beam Experiments

- Most experiments today are done with colliding beams

- CDF (Fermilab)
- D0 (Fermilab)
 - $p\bar{p}$ @ 1 TeV/beam
 - highest energy in world - currently



- BaBar (SLAC) $3 \text{ GeV } e^+ \otimes 9 \text{ GeV } e^-$
 - B Factory

The Standard Model

A very successful model of elementary particles and their interactions was been developed (~1970s). It has stood up to all experimental tests, but we know it is incomplete

- The fundamental fermions
- The interactions
- The limitations

The Fundamental Fermions

- All matter is built from small number of fermions (spin 1/2) particles
- Leptons (integer charge) - six 'flavors'
 - charged leptons (electron, muon, tau)
 - $\tau(\text{muon}) = 2.2 \text{ microsec}$ $\tau(\text{tau}) = 0.3 \text{ picosec.}$
 - neutral leptons (electron-neutrino, muon-neutrino, tau-neutrino)
- Quarks (fractional charge) - six 'flavors'
 - up-type quarks (up, charm, top)
 - down-type (down, strange, bottom)
 - only up and down are stable

The Fundamental Fermions

FERMIONS			matter constituents spin = 1/2, 3/2, 5/2, ...		
Leptons spin = 1/2			Quarks spin = 1/2		
Flavor	Mass GeV/c ²	Electric charge	Flavor	Approx. Mass GeV/c ²	Electric charge
ν_e electron neutrino	$<1 \times 10^{-6}$	0	u up	0.003	2/3
e^- electron	0.000511	-1	d down	0.006	-1/3
ν_μ muon neutrino	<0.0002	0	c charm	1.3	2/3
μ^- muon	0.106	-1	s strange	0.1	-1/3
ν_τ tau neutrino	<0.02	0	t top	175	2/3
τ^- tau	1.7771	-1	b bottom	4.3	-1/3

Fundamental Fermions in Nature

- Leptons exist as free particles
- Quarks have never been observed as free particles, only bound within composites, such as the proton (uud), the neutron (udd), the pion (u, anti-d), etc.
- This property of quarks is called 'confinement' and it is an important property of the strong interaction
- The stable particles are the lightest: the electron, u and d quarks, neutrinos.

The Interactions

- Strong
 - binds quarks, mediated by gluon (massless, spin 1)
- Electromagnetic
 - binds electrons in the atom (mediated by photon)
- Weak
 - responsible for β decay; mediated by $W^{\pm}$, Z^0 (massive, spin 1)
- Gravity
 - force between all matter, mediated by graviton (massless, spin 2)

The Interactions

	Gravity	Electromag.	Weak	Strong
field boson	graviton	photon	$W^\pm, Z$	gluon
spin-parity	2^+	1^-	$1^-, 1^+$	1^-
mass, GeV	0	0	$M_W=80.2$ $M_Z=91.2$	0
range, m	∞	∞	10^{-18}	$\leq 10^{-15}$
source	mass	electric charge	'weak' charge	'color' charge
coupling constant	5×10^{-40}	$1/137$	1.2×10^{-5}	≤ 1
typical cross- section, m^2		10^{-33}	10^{-39}	10^{-30}
typical lifetime, s		10^{-20}	10^{-10}	10^{-23}

Measuring the time scales

- Timescales of 10^{-10} seconds are straightforward, since particles typically travel at the speed of light, and distances of many mm are involved
- Shorter times can be more difficult
- Consider the time scale of the strong interaction:
 10^{-23} sec
 - for these particles, we must measure the 'width'
 $\Gamma = \hbar/2\pi\tau$ (uncertainty principle)

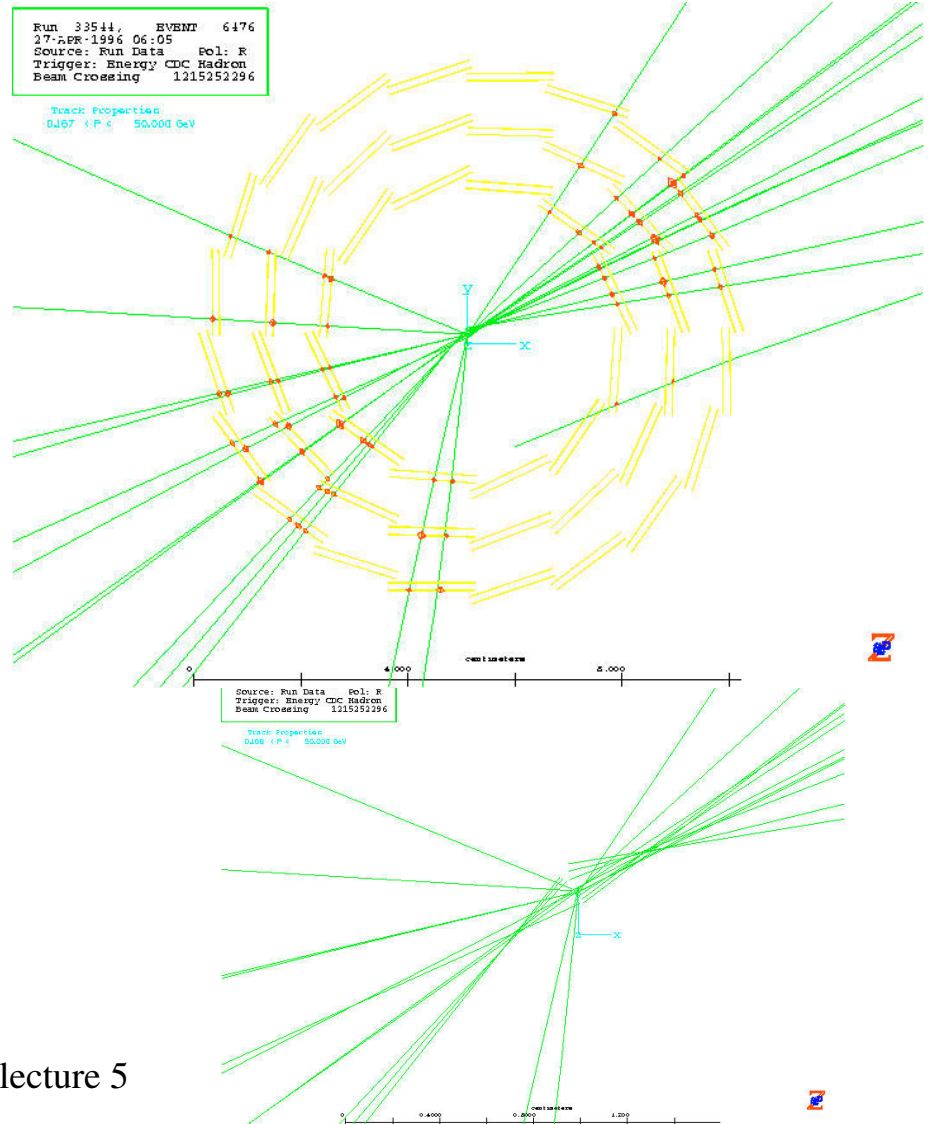
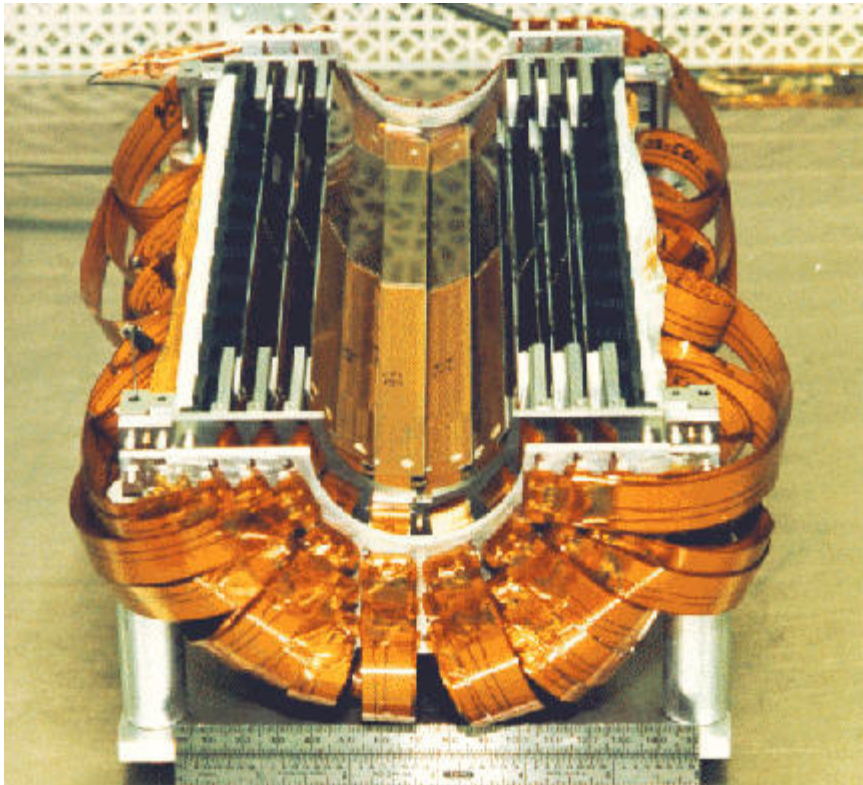
Measuring the time scales

- If a particle travels millimeters, we can measure its trajectory with precision detectors (vertex detectors)

$$\begin{aligned}d &= c \tau \\&= 3 \times 10^{10} \text{ cm/sec } \tau \\&= 3 \text{ mm} / 10^{-11} \text{ sec } \tau \\&= 3 \text{ mm } \tau / 10^{-11} \text{ sec}\end{aligned}$$

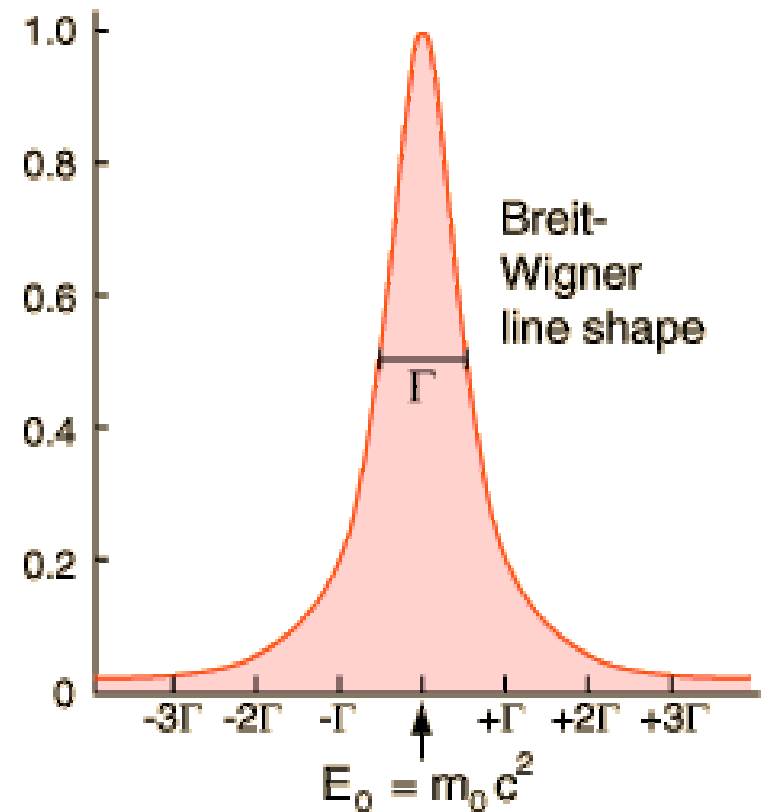
(we can actually measure sub-millimeter flight distances)

Vertex Detector



Measuring the time scales

- The uncertainty principle tells us that if we try to measure the mass of an unstable particle, there will be an uncertainty in that measurement
 - $\Delta E \Delta t > h/4\pi$
 - $\Gamma(\text{MeV}/c^2) = 7 \times 10^{-22} \text{sec} / \tau$



<http://230nsc1.phy-astr.gsu.edu/hbase/quantum/parlif.html>

The Limitations of the Standard Model

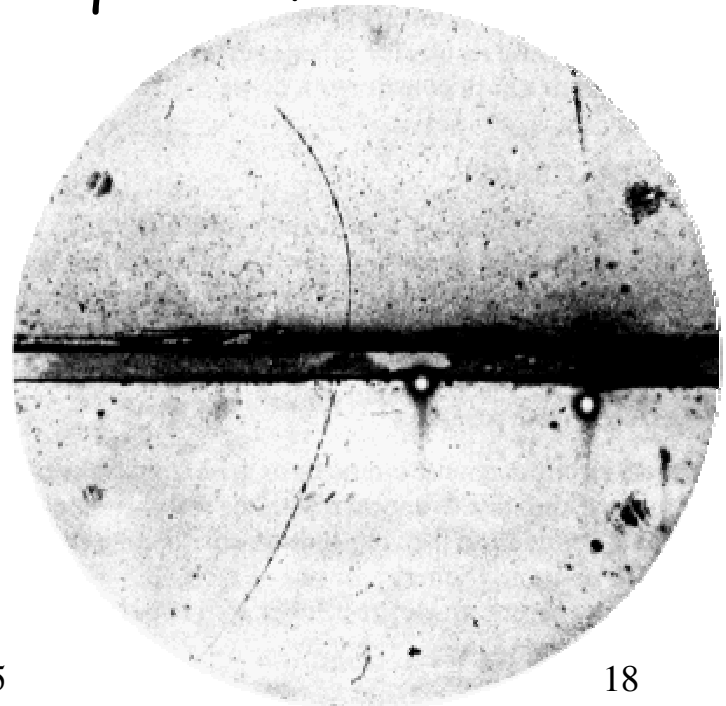
- Gravity is not explicitly included
- Neutrinos are assumed to be massless
- 17 arbitrary constants
 - masses (9) quarks and charged leptons
 - mixing angles (4) CKM matrix for the quarks
 - coupling constants (4) G_F , α , α_s , $\sin^2\theta_w$
- Six 'copies' of quarks and leptons assumed without understanding of reason for six
- Dark matter is not understood

Bosons and Fermions

- The fundamental particles are fermions (spin $1/2$), but bosons can be constructed from even numbers of the fund. fermions
- For example, the pions are bosons and obey bose-statistics
- The application of Fermi-Dirac and Bose-Einstein statistics is important in the study of the fundamental particles, and we will make use of it:
 - an example is the understanding of the $\Delta^{++} = (uuu)$ particle, which led to the realization of a new quantum number, color

The particles and antiparticles

- Every particle has a corresponding antiparticle, with the same mass and lifetime, and opposite charge and magnetic moment
- Dirac predicted this from fundamental considerations of relativity and quantum mechanics
- The first antiparticle, the positron, was discovered in 1932 in a cloud chamber experiment with cosmic rays



Particle and antiparticles

- Both bosons and fermions have antiparticles, however for fermions there is a conservation law: the difference in the number of fermions and antifermions is a constant
- This law is the origin of the conservation of baryons number and lepton family number:
 - $n \rightarrow p e^- \bar{\nu}_e$
 - $\pi^- \rightarrow \mu^- \bar{\nu}_\mu$
 - $\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu$

Particle and antiparticles

- This conservation law does not exist for bosons, so that the following reactions are all possible
 - $p p \rightarrow p p \pi$
 - $p p \rightarrow p p \pi \pi$
 - $p p \rightarrow p p \pi \pi \pi$
- A boson may be its own antiparticle
 - eq. π^0